

Affleck-Dine baryogenesis in large extra dimensions

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Baryogenesis in the models where the fundamental scale is as low as TeV in the context of large extra dimensions is a challenging problem. The requirement for the departure from thermal equilibrium necessarily ties any low scale baryogenesis with that of a successful inflationary model which automatically provides the out of equilibrium condition after the end of inflation. However, it is also noticeable that in these models the reheat temperature of the Universe is strongly constrained from the overproduction of Kaluza-Klein modes, which enforces a very low reheat temperature. In this paper we describe a possible scenario for baryogenesis which has a similar characteristics of an Affleck-Dine field. We notice that in order to have an adequate baryon to entropy ratio one requires to promote this Affleck-Dine field to reside in the bulk.

I. INTRODUCTION

Baryogenesis is an interesting offshoot of cosmology and particle physics, which tries to explain why the ratio of baryon density and photon density is given by one part in 10^{10} during the nucleosynthesis era [1]. The synthesis of light elements depends crucially on this ratio which tells us that in an absence of any observed anti-matter region, the baryon density should be equal to the cosmological baryon asymmetry. There are many proposals which can satisfy the three conditions; namely C and CP violation, B or L violation, and, out of equilibrium decay, which are the essential ingredients for baryogenesis [2]. Out of the three mentioned conditions the last one has to come purely from the cosmological evolution of the Universe. It is quite probable that the early Universe might have had strong departure from thermal equilibrium due to a large expansion rate of the Universe and presence of heavy decaying particles, however, this possibility gradually becomes difficult to acquire at scales which are comparable to the electroweak scale. As a second alternative, one might expect to attain the departure from thermal equilibrium via some phase transitions which would break global or gauge symmetry, a perfect example is electroweak phase transition where there is an anomalous $B + L$ violation, for a review, see Ref. [3]. In the former situation, the departure from thermal equilibrium is usually tied up with inflation. Inflation is an attractive paradigm which solves a range of troublesome problems of the Big Bang cosmology besides acting as the best candidate for producing an almost scale invariant density perturbations. After a period of inflation the Universe undergoes through an era of reheating, and this is precisely where one might expect to produce massive bosons and their out of equilibrium decay which might lead to the desired baryon to entropy ratio.

On the other hand recent trends in solving the hierarchy problem, in the context of theories with extra dimension, suggest that the strength of the fundamental scale, might be much lower than the four dimensional Planck scale. If that scale be the electroweak scale then the hier-

archy between the Planck scale and the electroweak scale can be inverted by assuming that there exists large extra dimensions, which can be as large as mm [4]. It is also assumed that the SM particles are trapped in a four dimensional hypersurface (a 3-brane), thus, they are not allowed to propagate in the bulk. However, it is generically assumed that besides gravity, SM singlets may propagate in the bulk. Among them the inflaton can be a candidate, which is less favored to be a brane field (see for instance Refs. [5,6]). However, in these models the Universe during the radiation dominated epoch reaches its maximum temperature very close to MeV which we shall discuss in details in the coming sections. For such a low reheat temperature baryogenesis is a challenging task because of two reasons; first of all the late decay of particles including the inflaton which is responsible for reheating the Universe, and, secondly the operators which might lead to baryon number violation must be suppressed due to stringent constraints on proton life time. This restricts us to a few choices of baryogenesis models which may work well in presence of a small fundamental scale, such as $\sim \mathcal{O}(\text{TeV})$ [7].

Other possibility may appear from the fact that reheat temperature is not the maximum temperature in the Universe after the end of inflation. Usually, reheating takes a while and it is possible to reach a temperature during the process of reheating which can be quite large, however, this rise in temperature crucially depends on the scale when inflation comes to an end [8]. If this be the case, then, it is quite possible that the rate of sphaleron transitions are active, even though the reheat temperature is much smaller than 100 GeV [9]. In this paper we describe a completely different possibility. This mechanism does not depend on the predictability of high rise in temperature during the reheating era. Our scheme is analogous to the Affleck-Dine (AD) mechanism of baryogenesis. We organize our paper with a brief discussion on reheat temperature and the bounds upon the reheat temperature, then we describe the possibility of leptogenesis which can be reprocessed into baryon number B by anomalous $B + L$ violating sphaleron interactions, which

otherwise preserve $B-L$. However, we also point out that there are many obstacles with this mechanism. Finally, we discuss baryogenesis by assuming a singlet carrying a *global charge* and decaying mainly into SM quarks and leptons to provide an adequate baryon to entropy ratio just at the end of reheating. Towards the end we conclude our paper by summarizing the facts.

II. REHEAT TEMPERATURE OF THE UNIVERSE

In models with a large extra dimensions, the reheat temperature is constrained from the possible thermal overproduction of gravitons in processes, such as; $\gamma + \gamma \rightarrow G$, which requires $T_r \lesssim 60$ MeV [7]. The second important observation is that the inflaton field in these models has a natural coupling to the SM fields which is Planck mass suppressed [5]. This is due to the fact that the inflaton field resides in the bulk. This helps to inflate the size of the extra dimensions from its natural size; $(\text{TeV})^{-1}$ to its present millimeter size in order to maintain the hierarchy, it also solves naturally the stabilization of the size of the extra dimensions [6], and, besides all, it can provide an adequate density perturbations required for the structure formation in the Universe. As a consequence, the inflaton has a decay rate into Higgses, for instance, given as [5]

$$\Gamma_{\phi \rightarrow \text{HH}} \sim \frac{g^2 M^3}{32\pi M_P^2}, \quad (1)$$

where g the coupling constant, M is the fundamental scale which is related to the size of the extra space; V_n , and, to the four dimensional Planck mass through [4]

$$M^{2+n} V_n = M_P^2. \quad (2)$$

For $n = 2$ extra dimensions M can be at a TeV range. Current experimental limits from collider physics and supernova 1987A imposes a bound; $M \gtrsim 30$ TeV [4,10].

While deriving the decay rate in Eq. (1), we have implicitly assumed that the mass of the inflaton is roughly of the order of the fundamental scale $\sim M$, in order to generate an adequate density fluctuations [5,6]. The estimated reheat temperature of the Universe is given by $T_r \sim 0.1 \sqrt{\Gamma M_P} \sim 1(10)$ MeV, just right above the temperature required for successful Big Bang nucleosynthesis. It is also worth mentioning that the decay rate of the inflaton field into the relativistic particles, such as light degrees of freedom has a similar suppression as Eq. (1). This is completely a different scenario than that of the standard case where Planck scale is the fundamental scale. For our case, the inflaton decay into the (non relativistic) Higgses is as favorable as decaying into very light particles. This makes a difference while discussing the maximum temperature reached during the reheating era, which is quite different from the reheat temperature of the Universe. As the inflaton field oscillates with a decaying amplitude, the Universe is gradually filled up

by the light degrees of freedom which produces an effective temperature of the Universe which follows a different scaling relationship between the temperature and the scale factor. The temperature reaches its maximum when $a/a_I \sim 1.48$, where a denotes the scale factor of the Universe and the subscript I denotes the era when inflation comes to an end. In the large extra dimension models, the inflationary scale is determined by $H_I \sim M$ [5,6]. After reaching the maximum temperature, it decreases as $T \sim 1.3(g_*(T_m)/g_*(T))^{1/4} T_m a^{-3/8}$, where T_m denotes the maximum temperature [8,9]. For $M \sim 10$ TeV, the maximum temperature could reach $T_m \sim 10^5$ GeV as mentioned in Ref. [9]. The basic assumption that goes behind this derivation is that the inflaton field is predominantly decaying into the relativistic species. However, this may not be the case. By reversing the argument, and, naively assuming that the inflaton decay populates only the non-relativistic degrees of freedom, one can show that the maximum temperature follows: $M \gtrsim T_m \gg T_r$, but, still much higher than the reheat temperature of the Universe. Note in this case the temperature-scale factor dependence, however, follows: $T \propto a^{-1}$. Whatsoever be the case eventually the massive particles have to decay into a radiation bath, the decay rate of these intermediate particles are now governed by their gauge couplings. If this happens the Universe might again be populated by radiation domination while the inflaton field is oscillating. This could again raise the maximum temperature above 100 GeV. Thus, the result apparently seems to be a robust one. This might be a cheerful news for the electroweak baryogenesis. However, it is still not clear whether the sphaleron transitions can be made useful for other sources of baryogenesis, such as leptogenesis. This is the topic we shall briefly meander upon before discussing the Affleck-Dine baryogenesis.

A. Leptogenesis

Following our previous discussion one might suspect that the lepton number being produced in the decay process of a heavy fermionic singlet which carries the lepton number, being processed into baryon number by anomalous $B + L$ violating sphaleron interactions which are in equilibrium for a temperature more than 100 GeV in the present circumstances. However, there is a simple catch in this proposal. A singlet right handed neutrino can naturally couple to the SM lepton doublet, and, the Higgs field in a following way: $h \bar{L} H N$. This leads to a potentially large Dirac mass term unless the Yukawa coupling $h \sim 10^{-12}$, or, so. Moreover, now the see-saw mechanism fails to work, since, the largest Majorana mass we may expect can never be larger than the fundamental scale. Therefore, given a neutrino mass $\sim h^2 \langle H \rangle^2 / M \sim h^2 \cdot \mathcal{O}(1)$ GeV, we still have to fine tune $h^2 \lesssim 10^{-10}$, in order to obtain the right order of magnitude for the neutrino mass. Thus, the right handed neutrinos, if they at all exist, are more likely to be bulk fields rather than brane fields. Since, in such a case the

volume suppression of the bulk-brane coupling naturally provides a small coupling [11]. In any case the decay rate of the right handed neutrino to the SM fields is suppressed by the smallness of h that gives rise to a decay rate which is similar to Eq. (1). This makes extremely difficult to realize baryogenesis, because, eventually when the right handed neutrino decays into the SM fields, the background temperature is of the order of the reheat temperature, and, by this temperature the sphaleron transition is not at all in equilibrium. The sphaleron transition rate is exponentially suppressed. So, a seemingly suitable lepton number might not even get converted to the baryons to produce the desired baryon asymmetry in the Universe.

On the other hand, it might be possible that sphalerons can reprocess a pre-existing charge asymmetry into baryon asymmetry [12] reflected in an excess of e_L over anti- e_R created during inflaton oscillations. This mechanism requires that $(B + L)$ -violating processes are out of equilibrium before e_R comes into chemical equilibrium, such that the created baryon asymmetry could be preserved. Again, this has to happen during, or, above 100 GeV. Nevertheless, it is important to notice that still decaying inflaton field certainly injects more entropy to the thermal bath, provided the inflaton dominantly decays into the relativistic degrees of freedom. So, an initially large baryon asymmetry has to be created in order to obtain the right amount of asymmetry just before nucleosynthesis. One can easily estimate the amount of dilution that the last stages of reheating era will produce. The entropy dilution factor is given by :

$$\gamma^{-1} = \left(\frac{s(T_r)}{s(T_c)} \right) = \left(\frac{g_*(T_r)}{g_*(T_c)} \right) \left(\frac{T_r}{T_c} \right)^3 \left(\frac{a(T_r)}{a(T_c)} \right)^3, \quad (3)$$

where s is the entropy and T_c denotes the electroweak temperature ~ 100 GeV. For a low reheat temperature as $T_r \sim 1$ MeV, the above expression gives rise to $\gamma^{-1} \gtrsim 10^{25}$. While calculating the ratio between the scale factors, we have used $T \propto a^{-3/8}$. Notice, that the lower bound appears, because, $g_*(T_c) > g_*(T_r)$. This is due to the contribution coming from the heavier Kaluza-Klein (KK) graviton modes, albeit, their masses are much smaller than T_c that may be produced in the thermal processes, such as photon-photon fusion. Usually, these heavy modes will decouple from the thermal bath right before nucleosynthesis. However, their contribution must be taken into account in the total relativistic degrees of freedom: $g_*(T_c) = g_*(T_r) + g_{*KK}$, which can be as large as the number of modes with masses between T_c and T_r ; thus giving, $g_{*KK} \lesssim R\Delta T \sim 10^{14}$, for $R \sim \text{mm}$. Strictly speaking the bound obtained on γ^{-1} in our case is true only if $g_{*KK} = 0$. Therefore, including the entropy dilution factor, one concludes that the initial n_b/s has to be extremely large $\gtrsim 10^{15}$, in order to produce the required baryon asymmetry during nucleosynthesis, which is $n_b/s \sim 10^{-10}$. Such a large baryon asymmetry is an extraordinary requirement on any natural model

of baryogenesis, which is almost impossible to achieve in our case.

There are couple of important lessons to be learned from the above analysis. First of all the large production of entropy during the last stages of reheating can in principle wash away any baryon asymmetry produced before electroweak scale. The second point is that it is extremely unlikely that leptogenesis will also work because one needs to inject enough lepton asymmetry in the Universe before the sphaleron transitions are in equilibrium. The only simple choice left is to produce directly baryon asymmetry, however, just before the end of reheating. The sole mechanism which seems to be doing well under these circumstances is the Affleck-Dine baryogenesis, which we shall discuss in the following section.

III. AFFLECK-DINE BARYOGENESIS

Affleck and Dine have proposed a beautiful scenario of baryogenesis in the context of supersymmetry [13]. A scalar condensate which carries non-zero baryonic, or/and leptonic charge survives during inflation and decays into SM fermions to provide a net baryon asymmetry. In our case the AD field; χ , is a singlet carrying some global charge which is required to be broken dynamically in order to provide a small asymmetry in the current density. This asymmetry can be then transformed into a baryonic asymmetry by a baryon violating interactions which we discuss later on. In order to break this $U(1)_\chi$ charge we require a source term which naturally violates CP for a charged χ field, and during the non-trivial helical evolution of the χ field generates a net asymmetry in χ over $\bar{\chi}$. This necessarily has to happen after the end of inflation. Notice, that in our case the initial CP phase is completely arbitrary and determined during the end of inflationary era.

We remind the readers that the inflaton energy density must govern the evolution of the Universe, and, the decay products of the inflaton is also responsible for reheating the Universe. This happens once the inflaton decays before χ decays into SM quarks and leptons. This decay of χ via baryon violating interaction generates a baryon asymmetry in the Universe which is given by

$$\frac{n_b}{s} \approx \frac{n_b}{n_\chi} \frac{T_r}{m_\chi} \frac{\rho_\chi}{\rho_I}. \quad (4)$$

The final entropy released by the inflaton decay is given by $s \approx \rho_I/T_r$. The ratio n_b/n_χ depends on the total phase accumulated by the AD field during its helical motion in the background of an oscillating inflaton field, which can at most be $\approx \mathcal{O}(1)$. If we assume that the AD field is a brane-field, then, the energy density stored in it can at most be: $\rho_\chi \approx m_\chi^2 M^2$, on the other hand the energy density stored in the (bulk) inflaton field is quite large $\rho_I \approx M^2 M_p^2$ [5,6]. Thus, the ratio: $n_b/s \sim (T_r/M_p)(m_\chi/M_p) \approx 10^{-34}(m_\chi/M) \ll 10^{-10}$, for $T_r \sim \mathcal{O}(1-10)$ MeV. The conclusion of the above analysis

is again disappointing, as it suggests that the AD baryogenesis also leads to a small n_b/s . One way to boost this ratio is to assume that the AD field resides in the bulk. In that case one naturally enhances the ratio ρ_χ/ρ_I , however, keeping in mind that it is still less than one, in order not to spoil the successes of inflation.

Once, the AD field is promoted to the bulk, the energy density stored in the AD field rises to $\rho_\chi \sim m_\chi^2 M_p^2$ [5,6], this leads to the *maximum* baryon to entropy ratio

$$\frac{n_b}{s} \approx \left(\frac{T_r}{M}\right) \left(\frac{m_\chi}{M}\right) \sim 10^{-10} \left(\frac{m_\chi}{1\text{GeV}}\right), \quad (5)$$

where we have evaluated the right hand side for $T_r \sim 10$ MeV and $M \sim 10$ TeV. Although, the mass of the AD field requires some fine tuning, up to the CP phase, the above ratio can reach the observed baryon to entropy ratio quite comfortably. Notice, however, that the actual predicted value also depends on the initial conditions on χ that may render m_χ more freedom. Say for instance, if $\chi_0 \sim M_{GUT}$, we get the right n_b/s provided $m_\chi \sim M$.

We have noticed earlier that due to the violation of $U(1)_\chi$ charge, the dynamics of the AD field generates an excess of χ over $\bar{\chi}$ fields. This asymmetry is transferred into baryon asymmetry by a baryon violating interaction, such as $\kappa\chi QQQ L$, however, keeping $B - L$ conserved. We also assume that χ interactions to SM fields conserve $U(1)_\chi$ symmetry, thus, the quarks and leptons must carry a non zero global χ charge while the Higgs field does not. This avoids χ decaying into Higgses, which otherwise will reduce the baryonic abundance and make the above interaction the main channel for its decay. While discussing the decay rate of χ field one has to take into account all possible decay channels which can be of the order of thousands due to family and color freedom. On the other hand, we assume that the inflaton is decaying mainly into Higgses. Final result is then given by

$$\Gamma_\chi \approx \left(\frac{\kappa}{g}\right)^2 \left(\frac{m_\chi}{M}\right)^7 \Gamma_\phi. \quad (6)$$

By taking $\kappa/g \sim \mathcal{O}(1)$ we can insure that χ will decay along with the inflaton, provided that its mass is very close to the fundamental scale. This will certainly demand some level of fine tuning in the parameters. We would like to mention that this is perhaps the simplest scenario one can think of for generating baryon asymmetry right before nucleosynthesis takes place. It is worth mentioning that in our model the AD field will not mediate proton decay by dimension six operators as $QQQL$, as long as χ does not develop any vacuum expectation value. Notice, other processes mediating proton decay, such as instanton effects might still occur. While there is no known solution for such a potential problem yet, our mechanism is at least not adding any new source to proton decay. In the same spirit one may check those operators which induce $n - \bar{n}$ oscillations. Again, effective $\Delta B = 2$ operators of dimensions 9; $UDDUDD$, and 11; $(QQQH)^2$, can not be induced by integrating out χ .

IV. CONCLUSION

We have noticed that the observed baryon asymmetry in the Universe is difficult to obtain in presence of a large extra dimensions. We have pointed out that there is a seemingly simple way, if we assume that there exists a SM singlet field carrying some global $U(1)_\chi$ charge which lives in the bulk. The non trivial dynamics of this field generates an asymmetry in $\chi - \bar{\chi}$ after the end of inflation, which will be transferred into a baryon asymmetry by a baryon violating interaction. It is possible to insure that the AD field decays along with the inflaton such that the synthesis of the light elements can take place.

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